## Rounding answers

The table shows the numbers of various A-level grades achieved by female and male candidates in England, Wales and Northern Ireland in one particular year, together with the total number of entries. Using a calculator, express the numbers given for A-grades and Bgrades for females as percentages of the number of female entries, and the numbers given for A -grades and B -grades for males as percentages of the number of male entries: (a) to the nearest percent, (b) to one decimal place, (c) to two decimal places. Which of these seems the most appropriate way to give the percentages?

| Grades | A | B | C | D | E | N | U | No. of entries |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Females | 58364 | 67566 | 75318 | 70680 | 54849 | 31673 | 27811 | 386261 |
| Males | 57125 | 57469 | 63664 | 61580 | 48178 | 29270 | 26842 | 344128 |

## Answers to check-up 16

a) Females: A-grades $15 \%$, B-grades $17 \%$. Males: A-grades $17 \%$, B-grades $17 \%$.
b) Females: A-grades $15.1 \%$, B-grades $17.5 \%$. Males: A-grades $16.6 \%$, B-grades 16.7\%.
c) Females: A-grades $15.11 \%$, B-grades $17.49 \%$. Males: A-grades $16.60 \%$, Bgrades $16.70 \%$.

It is probably appropriate to give the results to one decimal place, as in (b).

## Discussion and explanation of check-up 16

We often find ourselves in the position of having more figures in the result of a mathematical calculation than we can usefully use. A teacher calculating the result of a $3.5 \%$ increase in her salary of $£ 21,565$ might get the answer 22319.775 on her calculator, but would probably think of it as 'about $£ 22,300$ '. In such circumstances we often round answers to the nearest something, such as, in this case, to the nearest hundred pounds. Not always, of course. If I was calculating how many 68 -seater buses I needed for 370 pupils and adults going on a school trip ( $370 \div 68=5.4411764$ on my calculator), then rounding to the nearest whole number (5) would result in having to leave 30 passengers behind! The first important consideration, therefore, is the context that gave rise to the calculation. Especially when handling statistical data, however, it will often be appropriate to round answers to the nearest something, as in the example in this check-up.

My calculator gives the proportion of A-grades for males to be $16.599928 \%$. To round this to the nearest whole percent, we have to choose between $16 \%$ and $17 \%$. Halfway between these is $16.5 \%$. The answer is larger than this, so we round up to $17 \%$. To round $16.599928 \%$ to one decimal place, we have to choose between $16.5 \%$ and $16.6 \%$. Halfway between these is $16.55 \%$. The answer is larger than this, so we round up to $16.6 \%$. To round $16.599928 \%$ to two decimal places, we have to choose between $16.59 \%$ and $16.60 \%$. Halfway between these is $16.595 \%$. The answer is larger than this, so again we round up, to $16.60 \%$. Notice that it is important to give this answer as $16.60 \%$, not just $16.6 \%$, to indicate that it is correct to two decimal places.

What about rounding the proportion of A-grades for females (15.1099904\%)? To the nearest percent we round down to $15 \%$. To one decimal place we round
down to $15.1 \%$. Rounding to two decimal places we have to choose between $15.10 \%$ and $15.11 \%$. Halfway between these is $15.105 \%$. The answer is larger than this, so we round up to $15.11 \%$.

In deciding how many places to round to, we have to make sure we retain enough information to discriminate between different answers, but not so much that the figures become meaningless.

## Summary of key ideas

- To round an answer to a given number of decimal places:
- first decide between which two values with that number of decimal places the answer lies (e.g. 5.6481 lies between 5.64 and 5.65, to two decimal places)
- then note what comes halfway between these two values (e.g. 5.645)
- if your answer is greater than this, round up; if it is less, round down ( 5.6481 is greater than 5.645 , so round up to 5.65 ).

Always consider the context that gave rise to the calculation before rounding the answer.

- Give enough figures in the rounded results to be able to discriminate effectively between the data; but not so many that the data is difficult to take in and evaluate at a glance.


## Further practice

16.1 Using a calculator, express the proportions of C-grades, D-grades, Egrades and N -grades in the table in Check-up 16 as percentages, rounding them to one decimal place.
16.2 Why would it not be appropriate to give these proportions to the nearest whole percent? For example, look at the male and female results for D-grades and those for N -grades.

